

Oxygen isotopic ratios in intermediate-mass red giants

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ABSTRACT

Context. The abundances of the three main isotopes of oxygen are altered in the course of the CNO-cycle. When the first dredge-up mixes the burning products to the surface, the nucleosynthesis processes can be probed by measuring oxygen isotopic ratios.

Aims. By measuring $^{16}\text{O}/^{17}\text{O}$ and $^{16}\text{O}/^{18}\text{O}$ in red giants of known mass we compare the isotope ratios with predictions from stellar and galactic evolution modelling.

Methods. Oxygen isotopic ratios were derived from the *K*-band spectra of six red giants. The sample red giants are open cluster members with known masses of between 1.8 and 4.5 M_{\odot} . The abundance determination employs synthetic spectra calculated with the COMARCS code. The effect of uncertainties in the nuclear reaction rates, the mixing length, and of a change in the initial abundance of the oxygen isotopes was determined by a set of nucleosynthesis and mixing models using the FUNS code.

Results. The observed $^{16}\text{O}/^{17}\text{O}$ ratios are in good agreement with the model results, even if the measured values do not present clear evidence of a variation with the stellar mass. The observed $^{16}\text{O}/^{18}\text{O}$ ratios are clearly lower than the predictions from our reference model. Variations in nuclear reaction rates and mixing length parameter both have only a very weak effect on the predicted values. The $^{12}\text{C}/^{13}\text{C}$ ratios of the *K* giants studied implies the absence of extra-mixing in these objects.

Conclusions. A comparison with galactic chemical evolution models indicates that the $^{16}\text{O}/^{18}\text{O}$ abundance ratio underwent a faster decrease than predicted. To explain the observed ratios, the most likely scenario is a higher initial ^{18}O abundance combined with a lower initial ^{16}O abundance. Comparing the measured $^{18}\text{O}/^{17}\text{O}$ ratio with the corresponding value for the ISM points towards an initial enhancement of ^{17}O as well. Limitations imposed by the observations prevent this from being a conclusive result.

Key words. Nuclear reactions, nucleosynthesis, abundances – Stars: abundances – Stars: evolution – Stars: late-type

1. Introduction

The ratios of the abundances of the three stable isotopes of oxygen, $^{16}\text{O}/^{17}\text{O}$ and $^{16}\text{O}/^{18}\text{O}$, are important indicators of the nucleosynthesis and mixing in the interiors of stars (Dearborn 1992). In an H-burning environment $^{16}\text{O}(p,\gamma)^{17}\text{F}(\beta^+)^{17}\text{O}$ causes a steep increase in the ^{17}O abundance until equilibrium is reached by the competitive $^{17}\text{O}(p,\alpha)^{14}\text{N}$ process (Landre et al. 1990). Owing to the steep abundance gradient of ^{17}O resulting from incomplete CNO-cycle burning, the surface abundance of the ^{17}O isotope is highly sensitive to the precise depth of convection and the mixing profile in red giants (Boothroyd & Sackmann 1999). ^{18}O is primarily produced via $^{14}\text{N}(\alpha,\gamma)^{18}\text{F}(\beta^+)^{18}\text{O}$ (e.g. Clayton 2003). This reaction takes place in the He-burning shells of massive stars. The isotope is destroyed in hydrogen-burning stars by $^{18}\text{O}(p,\alpha)^{15}\text{N}$ and destroyed during He burning by $^{18}\text{O}(\alpha,\gamma)^{22}\text{Ne}$. In low and intermediate mass stars, the ^{18}O abundance thus reflects the initial abundance of this isotope and its destruction rate during hydrogen burning. The reaction rates for the processes including the various oxygen isotopes are relevant for later steps

in the stellar nucleosynthesis, in particular the s-process (see the discussion in, e.g., Straniero et al. 2014).

The solar values for $^{16}\text{O}/^{17}\text{O}$ and $^{16}\text{O}/^{18}\text{O}$ are 2700 and 498 (Lodders et al. 2009), respectively. Based on the interplay between the production, mixing, and destruction of the oxygen isotopes, stellar evolution models predict a correlation between oxygen isotopic ratios and stellar mass for red giants after the first dredge-up (Boothroyd et al. 1994; El Eid 1994; Stoesz & Herwig 2003; Karakas & Lattanzio 2014). The various models agree on a steep decrease in the ratio $^{16}\text{O}/^{17}\text{O}$ between 1 and around 2 M_{\odot} followed by a weak increase in this ratio for higher masses. At the same time, the $^{16}\text{O}/^{18}\text{O}$ value after the first dredge-up is expected to show a moderate increase for stars below 2 M_{\odot} and a constant value afterwards. There are small quantitative differences for the predicted $^{16}\text{O}/^{18}\text{O}$ ratio between the models. A direct comparison of abundances is hampered by variations in the starting values chosen by the various models.

For testing the predictions, RGB stars of known mass are crucial. El Eid (1994) attempted to do such a comparison with the help of a set of bright field stars. However, as noted by the author of that study, masses are rather uncertain for these objects. Accordingly, a convincing observational test of the models was not possible.

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The CO vibration-rotation $4.6\ \mu\text{m}$ fundamental or $2.3\ \mu\text{m}$ first overtone bands were used in early determinations of O isotopes in red giants. The early determinations were limited to bright stars due to instrumental constraints (see Harris et al. 1988; Smith & Lambert 1990, and references therein). Contemporary instrumentation is much more sensitive, allowing the study of weaker targets at high spectral resolution and high S/N. It is now possible to observe open-cluster (OC) red giants where stellar mass can be determined from the cluster age. Exploring the causes for oxygen isotopic ratios that deviate significantly from predictions based on the solar value provides insight into the cosmic matter cycle.

2. Sample definition and observations

For the target selection, we chose the list of red giants in galactic OC provided by Gilroy (1989) plus two stars in NGC 7789 from Prugniel et al. (2011). The total sample selected on the basis of observability (see below) and stellar mass includes seven stars. Gilroy (1989) provides the masses of the stars on the giant branch, and we used these values for our analysis. For NGC 7789 there are two recent age determinations of 1.4 Gyr (Kalirai et al. 2008) and 1.8 Gyr (Jacobson et al. 2011). When using isochrones from Bressan et al. (2012), the turn-off mass is $1.8 \pm 0.2 M_{\odot}$. The metallicities of the selected clusters are close to solar (Gilroy 1989; Prugniel et al. 2011). Our sample of red giants is listed in Table 1.

Subsequent to taking the observations, we found that HD 49050 is no longer considered a member of NGC 2287 (Mermilliod et al. 2008). On the other hand, cluster membership of HD 16068 in Tr 2 and HD 27292 in NGC 1545 was confirmed by Zács et al. (2011). For HD 68879, Frinchaboy & Majewski (2008) list a cluster membership probability of more than 96 %. For the other stars, their radial velocities are very close to the respective mean cluster velocity (Mermilliod et al. 2008), which supports their membership. A re-examination of the kinematics of the UMa group based on Hipparcos data leaves the membership of HD 30834 unclear (King et al. 2003).

We obtained several small pieces of high-resolution spectra in the H and K bands using the Phoenix spectrograph (Hinkle et al. 2000) at the Kitt Peak 2.1m telescope. Observations were obtained in December 2013 and January 2014. The standard infrared observing procedure with two nodding positions was applied. Telluric lines were removed by ratioing the spectra to spectra of hot stars observed at similar airmass. The telluric lines in the hot star spectra were also used for the wavelength calibration.

3. Isotopic ratios

Our goal was to derive the $^{16}\text{O}/^{17}\text{O}$, $^{16}\text{O}/^{18}\text{O}$, and $^{12}\text{C}/^{13}\text{C}$ ratios for our seven target stars. Owing to the very limited spectral range of about $100\ \text{\AA}$ covered by a single observation, the number of spectral features available for our analysis is smaller than in the earlier studies based on FTS scans of the whole K -band region. To measure the ^{17}O abundance we used two to four 2-0 band C^{17}O lines located near $4285.4\ \text{cm}^{-1}$. These lines are largely unblended and can be easily identified for a stellar temperature of up to 4200 K.

Determining the ^{18}O abundance from K -band spectra is more difficult. We ultimately used a region around $4226\ \text{cm}^{-1}$, which was used by García-Hernández et al. (2010) for their study of oxygen isotopes in R CrB stars. The most usable line of C^{18}O in

this region is the 2-0 R23 line, which is not affected significantly by telluric lines. However, this line is affected by an unidentified blend, so its usability for abundance determination is limited to $T_{\text{eff}} < 4100\ \text{K}$ and $\log g < 2.0$. An attempt to use the 2-0 band head of C^{18}O , as in Smith & Lambert (1990), for instance, failed since the band head is located too close to the transmission cut-off of the Phoenix order separation filter.

Complimentary information on mixing in the stellar atmosphere was derived by measuring the $^{12}\text{C}/^{13}\text{C}$ ratio for our sample stars. Several first overtone $^{12}\text{C}^{16}\text{O}$ and $^{13}\text{C}^{16}\text{O}$ lines near $4246\ \text{cm}^{-1}$ and $4262\ \text{cm}^{-1}$ were used. We also attempted observations of the CO fundamental spectrum near $4.6\ \mu\text{m}$ where many CO lines from all three oxygen isotopes can be found. However, lower flux levels, line blending, and difficulties in setting the continuum level limited the use of these data. The data presented in this paper are part of a larger observing programme on oxygen abundances in cool red giants. Details will be presented elsewhere.

Isotopic ratios were computed using spectrum synthesis techniques. For the stellar atmospheric structure, we used the hydrostatic spherical COMARCS models described in Aringer et al. (2009). Synthetic spectra were calculated with the COMA code using the same set of opacity data. Calculations were done under the assumption of LTE. We adopted values for solar composition provided by Caffau et al. (2009). Abundances were determined by a direct comparison between observed and synthetic spectra using both visual inspection and the measured line depths. For a more detailed description of our approach, we refer to earlier applications to the fitting of similar high resolution spectra given in Lebzelter et al. (2008) and Lederer et al. (2009). Line positions throughout the studied spectral range have been improved by using the work of Hinkle et al. (1995) and Hase et al. (2010). Data for the lines used in this analysis are listed in Table A.1.

The line strengths depend on the stellar temperature, surface gravity, chemical composition, and abundance of each isotope. For the stars taken from the list of Gilroy (1989), we used the values for T_{eff} and $\log g$ given there. McDonald et al. (2012) independently determined T_{eff} values for HD 27292 (3844 K), HD 30834 (4247 K), and HD 68879 (4552 K), which are in reasonable agreement with the values given by Gilroy¹. For the two stars in NGC 7789, the stellar parameters were taken from the study of Prugniel et al. (2011). Since all clusters have a metallicity close to solar (Gilroy 1989; Jacobson et al. 2011; Milone et al. 2011), we calculated our grid of synthetic spectra only for solar composition. For C/O we chose a fixed value of 0.3 to resemble a typical value for post first dredge-up composition. The microturbulence ξ was set $2.0\ \text{km s}^{-1}$, which is a typical value for these stars according to Gilroy (1989). The macro turbulence was set to values between 1.5 and $2.5\ \text{km s}^{-1}$ to optimize the fit of all stellar lines within the observed wavelength range. All parameters taken from the literature were cross-checked and confirmed with our spectra. The finally chosen values for T_{eff} and $\log g$ are given in columns 4 and 5 of Table 1. Examples for the spectral fit are shown in Figs. 1 and 2. We note that our synthetic spectra cannot fit the cores of the strongest CO lines (lowest excitation) properly (e.g. Fig. 1). This difficulty has also been encountered by other authors (e.g. Tsuji 2008) and likely results

¹ Cesetti et al. (2013) list a rather high temperature of 6427 K for HD 16068. They refer to a parameter determination by Holmberg et al. (2008). However, we could not find this star in the latter catalogue. Therefore, we suppose there is a mistake in Cesetti et al. (2013).

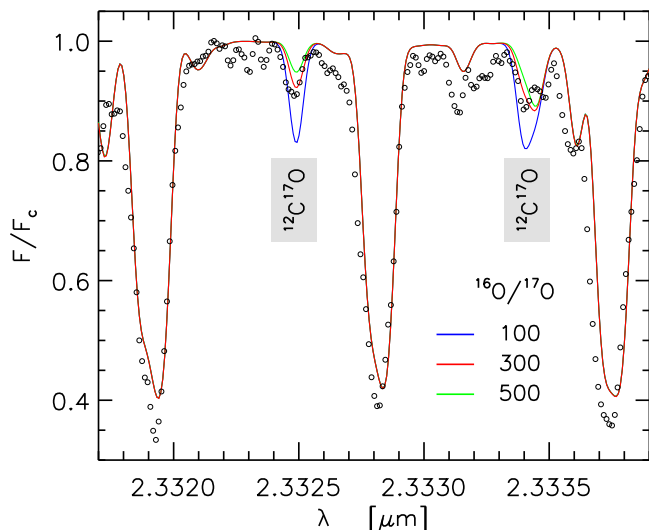


Fig. 1. Observed spectrum of HD 27292 (dots) showing two $^{12}\text{C}^{17}\text{O}$ lines. The three synthetic spectra (solid lines) are for $T_{\text{eff}}=4000$ K and $\log g=1.5$ with $^{16}\text{O}/^{17}\text{O}=100, 300$, and 500 .

from limitations of hydrostatic model atmospheres in describing the outer layers of a red giant properly.

The resulting oxygen isotopic ratios are listed in Table 1. The two stars in the cluster NGC 7789 show similar values. For the hottest star in our sample, HD 68879, we could not determine $^{16}\text{O}/^{17}\text{O}$ and $^{16}\text{O}/^{18}\text{O}$ because the CO lines were too weak. For HD 30834 we could not measure $^{16}\text{O}/^{18}\text{O}$ because the contribution of the C^{18}O line to the blend could not be constrained properly. For this star, the value given for $^{16}\text{O}/^{18}\text{O}$ in Table 1 is a lower limit. We also determined carbon isotopic ratios for all our stars. The carbon isotope results are in good agreement with the values determined by Gilroy (1989) (see Table 1).

To interpret the $^{16}\text{O}/^{17}\text{O}$ and $^{16}\text{O}/^{18}\text{O}$ ratios, we need to check whether a solar ^{16}O abundance value is appropriate for our sample stars. We did this by computing model spectra with altered oxygen abundances and with stellar parameters and carbon isotopic ratio as derived in the previous step. Since $\text{C}/\text{O} < 1$ the strengths of the CO lines are dependent on the carbon abundance and the isotopic ratios of oxygen but not on the total oxygen abundance. To derive the oxygen abundance, OH vibration-rotation lines in the H band were modelled. The H -band spectra around 6072cm^{-1} were obtained for six of the K giants in Table 1. We modelled the three least blended ^{16}OH lines, $4-2\text{P}_{1f} 6.5$, $2-0\text{P}_{1f} 16.5$, and $2-0\text{P}_{2e} 15.5$. The resulting abundances listed in Table 1 were all sub-solar by -0.16 to -0.36 dex. The uncertainties are dominated by the temperature sensitivity of the chosen OH lines. As noted above, the total oxygen abundance has no effect on the strengths of the CO lines. We also do not expect that the oxygen abundance will affect the atmospheric structure because photospheric H_2O is not present in the temperature range of our sample stars.

According to Gilroy (1989), the uncertainties of the stellar parameters are $\Delta T_{\text{eff}} \pm 150$ K, $\Delta \log g \pm 0.3$, $\Delta \xi \pm 0.2\text{km s}^{-1}$, and $\Delta [\text{Fe}/\text{H}] \pm 0.2$. Alternative parameter values found in the literature agree within these error bars. For each star we derived the isotopic ratios by changing the stellar parameters within these ranges. Some combinations, however, were not included when estimating the uncertainties because the corresponding synthetic spectra do not provide a good fit to the observations. Since the continuum level in the K band is well defined for these stars, we

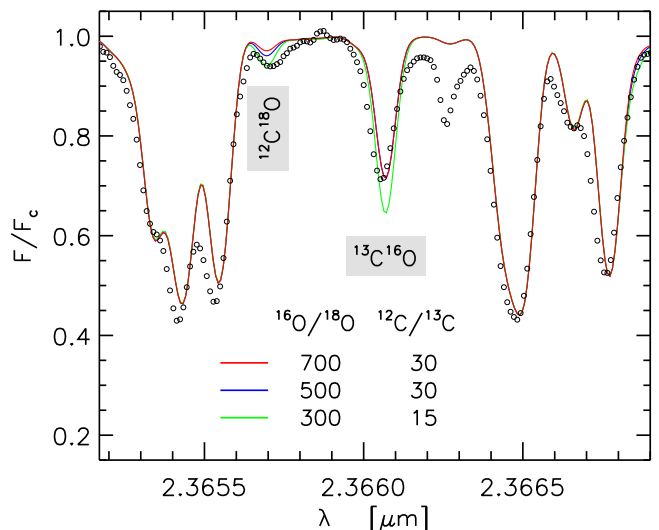


Fig. 2. Observed spectrum of HD 27292 (dots) with a $^{12}\text{C}^{18}\text{O}$ line and a $^{13}\text{C}^{16}\text{O}$ line marked. The three synthetic spectra (solid lines) are for $T_{\text{eff}}=4000$ K and $\log g=1.5$ with $^{16}\text{O}/^{18}\text{O}=300, 500$, and 700 and $^{12}\text{C}/^{13}\text{C}=15$ and 30 , respectively.

did not consider it to have an impact on the error budget. The final uncertainties, given in Table 1, were then determined by combining the maximum differences from changes in the stellar parameters with the scatter resulting when various lines were used for the abundance determination. The latter was typically a factor of 2 smaller than the uncertainties from the stellar parameters. As noted above we did not determine the C/O ratios from our spectra but set them to a fixed value of 0.3 in our analysis. We explored the effect of changing the C/O ratio by ± 0.1 dex on the derived oxygen isotopic ratios. Such a change somewhat modifies the strength of all CO lines, but primarily those of weak or moderate strength. To achieve a good fit of the whole spectrum again, the stellar parameters have to be adapted so that the net effect on the isotopic ratios is small and covered by the error budget derived above. The effect of changing the macro-turbulence value by 1km s^{-1} is a few percent on the resulting isotopic ratio.

For HD 16068 and HD 27292, we also observed the M -band spectrum near 2154cm^{-1} . As mentioned above, the M -band spectra could not be used to derive reliable isotopic ratios. However, attempting to achieve a reasonable fit to the $4.6\mu\text{m}$ spectra limits the $^{16}\text{O}/^{17}\text{O}$ and $^{16}\text{O}/^{18}\text{O}$ ratios to a range between 200 and 600, in agreement with the findings from the K band.

4. Nucleosynthesis and mixing models

To interpret the measured oxygen isotopic ratios, we have computed a set of stellar models by means of the FUNS (FULL Network Stellar evolution) code (Straniero et al. 2006). In practice, all the stable isotopes from H to F have been explicitly included in the H-burning nuclear network coupled to the stellar structure equations. The reaction rates have been taken from Iliadis et al. (2010) and Adelberger et al. (2011). The mixing length parameter, $\alpha=1.82$, was calibrated by means of a standard solar model computed with the same set of nuclear reaction rates, equation of state, radiative opacities, and composition as the models used in this study. Initial metallicity ($Z=0.015$) and He abundance ($Y=0.27$) are the early solar values as derived from the same standard solar model. The solar composition was taken

Table 1. Stellar parameters and isotopic ratios. Data in columns 3 to 6 are taken from the literature.

Cluster	Star	Mass [M_{\odot}]	T_{eff} [K]	$\log g$	$^{12}\text{C}/^{13}\text{C}$ Lit.	Ref.	[$^{16}\text{O}/\text{H}$]	$^{16}\text{O}/^{17}\text{O}$	$^{16}\text{O}/^{18}\text{O}$	$^{12}\text{C}/^{13}\text{C}$
NGC 7789	971	1.8 ± 0.2	3700	1.2	–	(2)	-0.18 ± 0.1	300^{+100}_{-70}	340^{+150}_{-50}	15 ± 8
	415	1.8 ± 0.2	3800	1.2	–	(2)	-0.16 ± 0.1	250^{+100}_{-70}	270^{+150}_{-40}	19 ± 8
NGC 2548	HD 68879	2.6 ± 0.3	4600	2.2	25	(1)	–	–	–	16 ± 7
NGC 1545	HD 27292	2.8 ± 0.2	4000	1.5	25	(1)	-0.33 ± 0.1	240^{+90}_{-50}	340^{+110}_{-70}	27 ± 10
UMa Grp.	HD 30834	2.9 ± 0.4	4000	2.2	26	(1)	-0.36 ± 0.1	260^{+90}_{-50}	>200	22 ± 7
NGC 2287	HD 49050	– ^a	4100	1.6	23	(1)	-0.19 ± 0.1	300^{+150}_{-50}	– ^b	30:
Tr 2	HD 16068	4.5 ± 0.4	4000	1.5	30	(1)	-0.28 ± 0.1	280^{+90}_{-50}	370^{+100}_{-90}	28 ± 10

References. (1) Gilroy (1989); (2) Prugniel et al. (2011).

Notes. ^(a) Star is probably not a cluster member. ^(b) S/N at the wavelength of the line too low.

from the list provided by Lodders et al. (2009). For details we refer to Piersanti et al. (2007). A comparison of FUNS predictions on stellar masses and cluster ages with the values derived by Gilroy (1989) showed good agreement within the uncertainties, so we refrained from re-determining the stellar masses of our sample stars. We point out that there is a minor inconsistency in our study in the sense that the oxygen abundance given by Lodders et al. (2009) is 0.07 dex lower than the value of Caffau et al. (2009) we used for computing the model spectra. Since the difference is very small, this inconsistency has negligible consequences on our analysis.

Stellar masses between 1.8 and $5.0 M_{\odot}$ have been investigated. The complete set of model parameter combinations and the corresponding results are summarized in Table 2. The first block (first 6 rows) refers to the reference models (R), those obtained with the recommended values of the reaction rates, the calibrated mixing length, and the solar composition. Then, to quantify the theoretical uncertainties, additional models have been computed by varying nucleosynthesis and mixing inputs, as well as the initial abundances of the three stable O isotopes.

As usual, all the models presented here include a treatment of the convective mixing. Therefore, red giant models show the composition modified by the first dredge-up. No extra mixing induced, for example, by rotation, thermohaline circulation, magnetic buoyancy, or gravity wave has been considered. As is well known these processes are hampered in red giant stars by the sharp molecular weight gradient left by the first dredge-up. Only in stars with $M \leq 2 M_{\odot}$ does the shell H-burning reach the H discontinuity during the RGB phase, thus smoothing down the μ – gradient. With the possible exception of the two NGC 7789 stars, all the other stars in our sample have masses higher than $2 M_{\odot}$. In the model with $M = 1.8 M_{\odot}$, the H-burning attains the H discontinuity when $\log(L/L_{\odot}) \sim 2$. The two giant stars observed in NGC 7789 are slightly brighter than this threshold² so some extramixing has possibly modified their compositions. However, the observed $^{12}\text{C}/^{13}\text{C}$ (Table 1) is only slightly smaller than the value expected after the FDU and, in any case, within the error bar. The O isotopic ratios are not affected by moderate extramixing (see, e.g., Abia et al. 2012).

² The luminosity may be estimated by means of T_{eff} and $\log g$ listed in Table 1.

5. Discussion

5.1. ^{17}O

All of the six sample K-giants with determined oxygen isotopic ratios show a very similar $^{16}\text{O}/^{17}\text{O}$ ratio between 250 and 300. Reference models, i.e. those obtained starting from a solar composition, account for the observed values within the observational errors. On the other hand, this agreement does not necessarily imply that the protostellar ^{17}O abundances were nearly solar. In the H-burning shell, the ^{17}O is directly linked to the ^{16}O through the NO cycle (see Figure 3). Therefore, the final $^{16}\text{O}/^{17}\text{O}$ is basically fixed by the initial abundance of the most abundant isotope of the cycle, ^{16}O , with variations of the initial ^{17}O having a negligible effect. This is demonstrated by model C17OH with an initial ^{17}O abundance 34% higher than the reference model but nonetheless a final $^{16}\text{O}/^{17}\text{O}$ ratio that is practically identical to the reference model. However, a variation in the initial ^{16}O will modify the isotope ratios after the first dredge-up. Nevertheless, a partial redistribution of the ^{16}O excess or deficiency over all the isotopes of the NO cycle mitigates the change in the final $^{16}\text{O}/^{17}\text{O}$. All the six giants in our sample show clear signatures of subsolar [$^{16}\text{O}/\text{H}$], with an average value -0.25 ± 0.03 (see Table 1). Models C16OL demonstrate that such a 40% reduction of the initial ^{16}O would imply a $\sim 14\%$ reduction of the final $^{16}\text{O}/^{17}\text{O}$ ratios, which is still compatible with the observed ratios (within 1σ ; see also the black-solid curve in Figure 4).

Variations in the nuclear reaction rates have weak effects compared to the observational uncertainties. A change of Z from 0.15 to 0.02 implies a 10% increase in the $^{16}\text{O}/^{17}\text{O}$. On the contrary, a 10% reduction is obtained if Y is changed from 0.27 to 0.32.

As a whole, at variance with model predictions, the measured $^{16}\text{O}/^{17}\text{O}$ ratios do not show any clear evidence of a variation with the stellar mass. However, the small number of observations, also affected by a rather large error, hampers any more thorough investigation of this issue. As outlined in Lebzelter et al. (2012), reducing the errors is hindered by fundamental problems in determining stellar parameters for cool giants. Effects of changes in the mixing length parameter are similarly far below the observational detectability.

5.2. ^{18}O

The models show that the $^{16}\text{O}/^{18}\text{O}$ ratio after the first dredge-up is almost constant (for $M \geq 2 M_{\odot}$). However, the five K-giants analysed here have typical values near 350, which is about half

Table 2. Effects of theoretical uncertainties on $^{12}\text{C}/^{13}\text{C}$, $^{16}\text{O}/^{17}\text{O}$, and $^{16}\text{O}/^{18}\text{O}$.

label	M (M_{\odot})	Initial isot. ratios			α_{ml}	Post-FDU isot. ratios			
		$^{16}\text{O}/^{17}\text{O}$	$^{16}\text{O}/^{18}\text{O}$	$^{17}\text{O}+\text{p}$ (rates)		$^{18}\text{O}+\text{p}$ (rates)	$^{12}\text{C}/^{13}\text{C}^a$	$^{16}\text{O}/^{17}\text{O}$	$^{16}\text{O}/^{18}\text{O}$
Reference models ^b									
R	1.8	2696	499	recom.	recom.	1.82	24.5	440	684
R	2.0	2696	499	recom.	recom.	1.82	24.2	262	703
R	2.5	2696	499	recom.	recom.	1.82	23.8	208	711
R	3.0	2696	499	recom.	recom.	1.82	23.5	253	709
R	4.0	2696	499	recom.	recom.	1.82	23.2	338	703
R	5.0	2696	499	recom.	recom.	1.82	22.9	381	704
Nuclear reactions changed ^c									
O17L	4.0	2696	499	low	recom.	1.82	23.2	320	704
O17H	4.0	2696	499	high	recom.	1.82	23.2	355	703
O17L	2.5	2696	499	low	recom.	1.82	23.8	193	711
O17H	2.5	2696	499	high	recom.	1.82	23.8	224	711
O18L	4.0	2696	499	recom.	low	1.82	23.2	336	681
O18H	4.0	2696	499	recom.	high	1.82	23.2	337	722
O18L	2.5	2696	499	recom.	low	1.82	23.8	210	693
O18H	2.5	2696	499	recom.	high	1.82	23.8	210	727
BL	2.5	2696	499	hi(γ),lo(α)	low	1.82	23.8	198	693
Initial composition changed ^d									
C17OH	2.5	2012	499	recom.	recom.	1.82	23.8	203	711
C18OH	2.5	2696	332	recom.	recom.	1.82	23.8	208	474
C18OHH	2.5	2696	249	recom.	recom.	1.82	23.8	209	356
C18OHH	3.0	2696	249	recom.	recom.	1.82	23.5	253	355
C18OHH	4.0	2696	249	recom.	recom.	1.82	23.2	336	352
C16OLL	2.5	1348	249	recom.	recom.	1.82	23.7	169	362
C16OLL	3.0	1348	249	recom.	recom.	1.82	23.5	203	361
C16OLL	4.0	1348	249	recom.	recom.	1.82	23.1	258	359
C16OL	1.8	1617	299	recom.	recom.	1.82	24.5	343	413
C16OL	2.0	1617	299	recom.	recom.	1.82	24.1	216	426
C16OL	2.5	1617	299	recom.	recom.	1.82	23.8	180	432
C16OL	3.0	1617	299	recom.	recom.	1.82	23.5	217	431
C16OL	4.0	1617	299	recom.	recom.	1.82	23.1	278	428
C16OL	5.0	1617	299	recom.	recom.	1.82	22.9	307	429
Mixing length parameters α_{ml} changed									
AL	2.5	2696	499	recom.	recom.	1.50	23.8	208	711
AH	2.5	2696	499	recom.	recom.	2.00	23.8	208	711
Metallicity change: Z=0.02									
Zvar	2.5	2696	499	recom.	recom.	1.82	23.6	189	723
He change: Y=0.32									
Yvar	2.5	2696	499	recom.	recom.	1.82	23.8	232	709

Notes. ^(a) Initial $^{12}\text{C}/^{13}\text{C}$ always set to 89. ^(b) Reference models as obtained by assuming solar composition (Lodders et al. 2009), O+p reaction rates from Iliadis et al. (2010) and solar-calibrated mixing length. ^(c) Models obtained using the lower and upper proton capture rates of ^{17}O or ^{18}O suggested by Iliadis et al. (2010). All other parameters equal to reference models. Model BL: capture rates setting chosen to minimize ^{18}O depletion. ^(d) Initial composition changed: $^{17}\text{O}\times 1.34$ (C17OH), $^{18}\text{O}\times 1.5$ (C18OH), $^{18}\text{O}\times 2$ (C18OHH), $^{16}\text{O}\times 0.5$ (C16OLL), $^{16}\text{O}\times 0.4$ (C16OL).

the value predicted by the reference models (R). None of the sample stars has an ^{18}O abundance in the literature. While our values seem to be amongst the lowest $^{16}\text{O}/^{18}\text{O}$ ratios measured in evolved giants, $^{16}\text{O}/^{18}\text{O}$ values around 400 have been measured in field giants. Harris et al. (1988) report similar values for the bright stars α Ari, α Ser, β And, β Peg, and β UMi. The Harris et al. (1988) study used different molecular lines than we have selected, which indicate that such low ratios are probably not the result of an inappropriate selection of spectral lines. All but one red giant studied by Harris et al. (1988) were found to have $^{16}\text{O}/^{18}\text{O}$ ratios ≤ 600 .

As for ^{17}O , our tests of the uncertainties of the nucleosynthesis model show that the only route to significantly modifying the $^{16}\text{O}/^{18}\text{O}$ ratio after the first dredge-up is to change the initial abundances of individual isotopes. At variance with the ^{17}O , for which only a variation in the initial ^{16}O abundance affects the final $^{16}\text{O}/^{17}\text{O}$, a modification of the initial ^{18}O could play an important role in interpreting the measured $^{16}\text{O}/^{18}\text{O}$ ratio. Owing to the weakness of the $^{17}\text{O}(p,\gamma)^{18}\text{F}$ reaction, ^{18}O remains decoupled from the CNO cycle (see Figure 3). On the other hand, it can be easily destroyed by fast proton captures (mainly by the $^{18}\text{O}(p,\alpha)^{15}\text{N}$ reaction) so that the $^{16}\text{O}/^{18}\text{O}$ ratio should in-

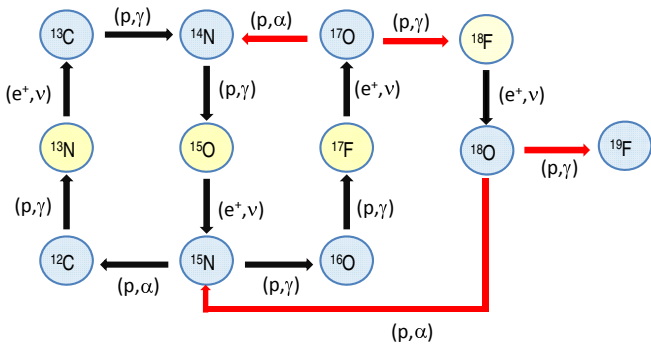


Fig. 3. Illustration of the network of nuclear reactions within the CNO cycle.

crease after the first dredge-up³. Our models show that for any choice of the initial ^{16}O , ^{18}O abundance pair and for any initial mass, the final $^{16}\text{O}/^{18}\text{O}$ will always be ~ 1.4 times greater than the corresponding initial value. For this reason, starting from a solar value of the $^{16}\text{O}/^{18}\text{O}$ ratio, ~ 500 , it is impossible to account for the measured values. Our models require that either the ^{16}O or the ^{18}O be varied in order to match the observations. For instance, model C18OHH with an initial ^{18}O twice solar abundance matches the observed $^{16}\text{O}/^{18}\text{O}$. However, this is also the result when using model C16OLL with an initial ^{16}O abundance half solar. It follows that combinations of these two assumptions also provide a good reproduction of the observations. For instance, assuming a 40% reduction of the initial ^{16}O , as implied by the observed average $[^{16}\text{O}/\text{H}]$, results in $^{16}\text{O}/^{18}\text{O}$, which is in reasonable agreement with the measured value (within 1σ ; Figure 5). The agreement can be improved further by increasing the initial ^{18}O about 10%.

5.3. Implications of the results

By combining $[^{16}\text{O}/\text{H}]$, $^{16}\text{O}/^{17}\text{O}$, and $^{16}\text{O}/^{18}\text{O}$ measurements in six giants belonging to galactic OC of known ages, we can infer the O isotopic composition of the respective protostellar nebulae. In particular, the optimal protostellar abundances modelled from the observed stellar abundances imply subsolar ^{16}O , i.e. -40% on the average, and slightly supersolar ^{18}O , i.e. $+10\%$. The $^{16}\text{O}/^{18}\text{O}$ ratios in the protostellar gas are reduced by a factor of ~ 1.4 from the values measured in the red giant stars. No direct information on the protostellar ^{17}O can be obtained from our observations.

Is this picture that arises from our measurements in OC giants compatible with the predictions of extant models of galactic chemical evolution⁴ (GCE)? ^{16}O is a primary product of the He burning. It is produced through the main He-burning chain: $3\alpha \rightarrow ^{12}\text{C} + \alpha \rightarrow ^{16}\text{O}$. ^{18}O is also produced in He-burning regions as a secondary product synthesized through the following chain: $^{14}\text{N}(\alpha, \gamma)^{18}\text{F}(\beta)^{18}\text{O}$, where the abundance of ^{14}N is equivalent, in practice, to the original amount of $\text{C} + \text{N} + \text{O}$. The most efficient polluters of both ^{16}O and ^{18}O are massive stars exploding as core-collapse supernovae. ^{17}O is a secondary product of the

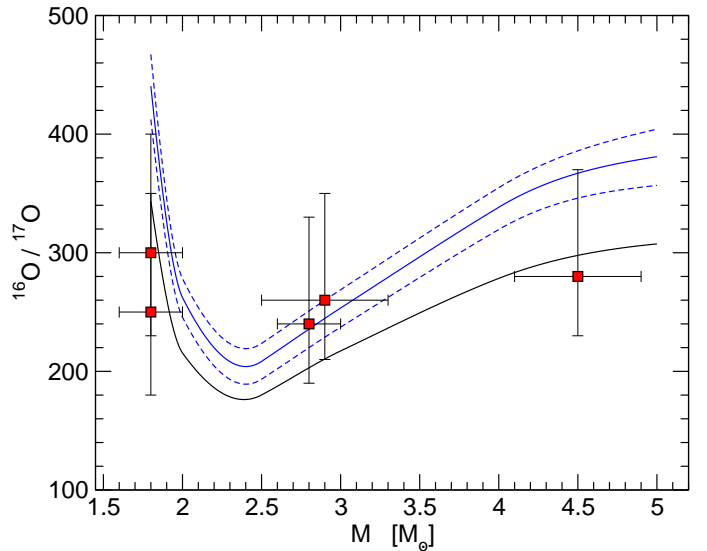


Fig. 4. $^{16}\text{O}/^{17}\text{O}$ ratios after the first dredge-up versus stellar mass in M_{\odot} . Lines represent the theoretical predictions, and the red squares are observations. Blue solid line: reference model (R). Blue dashed lines: ^{17}O proton capture rate modified within the suggested upper and lower rates (O17L and O17H). Solid black line: theoretical predictions as obtained by reducing the initial ^{16}O to $[^{16}\text{O}/\text{H}]=-0.22$ (C16OL).

H burning (CNO cycle, see Figure 3). Therefore, in addition to massive stars, the winds of intermediate and low mass stars contribute on a longer timescale to the oxygen pollution of the ISM by contributing ^{17}O . In this framework, it is not a surprise that GCE models generally predict an increase with time in both the $^{16}\text{O}/^{18}\text{O}$ and the $^{16}\text{O}/^{17}\text{O}$, as expected for the ratio of a primary to a secondary product. Less straightforward is the evolution of the ratio of the two secondary O isotopes. In general, when two secondary isotopes are produced by the same class of stars, their ratio should remain constant. However, this is not the case for $^{18}\text{O}/^{17}\text{O}$, which is expected to decrease when low and intermediate mass stars begin to contribute to the pollution of the lightest isotope (Clayton 1988; Prantzos et al. 1996; Meyer et al. 2008; Kobayashi et al. 2011; Nittler & Gaidos 2012).

In Figure 6 predictions of the Prantzos et al. (1996) GCE model are compared with our estimates of $^{18}\text{O}/^{16}\text{O}$ in the parent nebulae of the OC. The solid line represents the predicted evolution of the $^{18}\text{O}/^{16}\text{O}$ ratio over the past 6 Gyr. The CGE model refers to abundances in the interstellar medium (ISM) at the current solar galactocentric radius, $R_{GC} = 8.5$ kpc. The $^{18}\text{O}/^{16}\text{O}$ ratio is plotted relative to the solar value while time is scaled to the epoch of the solar system formation. Red squares show our isotope ratio estimates for the three clusters NGC 7789, NGC 1545, and Tr 2. In spite of the large uncertainties, it appears that the primordial gas of the three clusters underwent a faster increase in the ^{18}O abundance than predicted from the GCE model. This figure does not change by using the more recent Kobayashi et al. (2011) GCE model. The galactocentric distance of the three clusters is only slightly greater than solar, between 9 kpc and 9.7 kpc. Although migration of the Sun and the clusters⁵ from small galactocentric radius cannot be excluded, the birthplaces should be within $6 < R_{GC} < 10$ kpc.

Oxygen isotopic ratios in molecular clouds located in this portion of the Galaxy are available from infrared and ra-

³ As previously noted ^{16}O is practically unaffected by the first dredge-up.

⁴ Isotopic ratios of oxygen measured in stars are typically given as $^{16}\text{O}/^{xx}\text{O}$ in the literature. Accordingly, we used this format of the isotopic ratio in the first part of the paper. Galactic chemical evolution models, however, often give the reversed ratio $^{xx}\text{O}/^{16}\text{O}$. Therefore, we decided to use $^{xx}\text{O}/^{16}\text{O}$ in this section to allow for an easier comparison with the literature.

⁵ Effects of migration are probably small for the two younger clusters, NGC 1545 and Tr 2, while it cannot be excluded in the case of NGC 7789 (1.7 Gyr old).

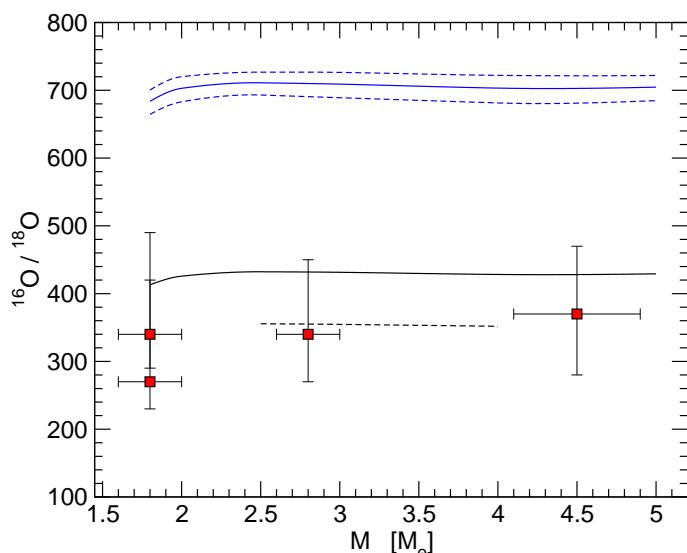


Fig. 5. $^{16}\text{O}/^{18}\text{O}$ ratios after the first dredge-up versus stellar mass in M_{\odot} . Lines represent the theoretical predictions, and the red squares are observations. Solid blue line: reference model (R). Dashed blue lines: ^{18}O proton capture rate modified within the suggested upper and lower rates (O18L and O18H). Solid black line: model predictions obtained by reducing the initial ^{16}O to $^{16}\text{O}/\text{H} = -0.22$ (C16OL). Dashed black line: model with the initial ^{18}O abundance increased by a factor of 2 (C18OHH).

dio observations (Wouterloot et al. 2008; Milam et al. 2005; Polehampton et al. 2005). Nittler & Gaidos (2012) have derived $^{18}\text{O}/^{16}\text{O}$ for molecular clouds by combining $^{13}\text{C}^{16}\text{O}/^{12}\text{C}^{18}\text{O}$ reported by Wouterloot et al. (2008) with the galactic $^{12}\text{C}/^{13}\text{C}$ gradient obtained by Milam et al. (2005) from CO observations. The two triangles in Figure 6 represent the weighted averages of these measurements, as obtained from two different molecular lines, CO J=1-0 and CO J=2-1. Only molecular clouds for $6 < R_{\text{GC}} < 10$ kpc have been considered. Other measurements, derived from OH lines (Polehampton et al. 2005) and formaldehyde data (Wilson & Rood 1994), are within the range covered by the CO measurements. In the same figure, the shaded area is representative of the whole set of available measurements for the ISM lying on the galactic disk approximately between 6 and 10 kpc (see also figure 2 in Nittler & Gaidos 2012). Compared to the ISM, the $^{18}\text{O}/^{16}\text{O}$ ratios we have derived for three OCs are close to the upper bound of the available measurements.

Although we cannot constrain the protostellar ^{17}O from OC giant observations, molecular clouds located between 6 and 1 kpc from the galactic centre show that the $^{18}\text{O}/^{17}\text{O}$ ratio ranges between 3 and 5, with an average value 4.16 ± 0.09 (Wouterloot et al. (2008); see also Penzias (1981) and Milam et al. (2005)). Since the ratio of these two secondary isotopes can either remain constant or decrease with time and since our measurements indicate slightly supersolar ^{18}O in the ISM from which the host clusters were born, a similar or even larger enhancement of ^{17}O is expected, otherwise the initial $^{18}\text{O}/^{17}\text{O}$ would be definitely too large compared to the typical values found in the galactic disk.

6. Conclusions

We measured the ratios of the three main isotopes of oxygen in the atmospheres of six evolved K giants. Except for one the stars are members of stellar clusters and therefore have well-defined

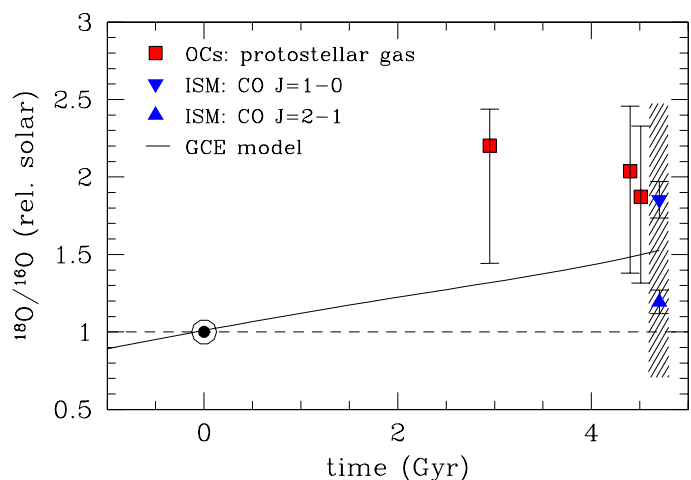


Fig. 6. Evolution of $^{18}\text{O}/^{16}\text{O}$ with time. The isotopic ratio is plotted relative to the solar value. The zero point of the time axis is defined by the formation of the sun. The solid black line indicates the predictions from galactic chemical evolution (GCE) models. Red boxes mark our estimates of $^{18}\text{O}/^{16}\text{O}$ in the parent nebulae of the three OCs NGC 7789, NGC 1545, and Tr2. The two measurements for NGC 7789 have been combined to one point. Blue symbols indicate ISM values. The shaded area is representative of the whole range of ISM measurements.

masses. The $^{16}\text{O}/^{17}\text{O}$ and $^{16}\text{O}/^{18}\text{O}$ ratios are compared with model predictions. There is agreement between observations and predictions for the $^{16}\text{O}/^{17}\text{O}$ ratio. The dependency of $^{16}\text{O}/^{17}\text{O}$ on mass, expected from nucleosynthesis models, is not observed. However, the predicted variation is comparable to the data errors. The observed $^{16}\text{O}/^{18}\text{O}$ ratio can be brought into agreement with model predictions if the initial isotopic ratio is about half of the solar value. Uncertainties in proton capture rates and mixing length cannot account for the observed difference. By combining this result with our estimation of the $^{16}\text{O}/\text{H}$, we conclude that a moderate enhancement of the initial ^{18}O abundance relative to the solar value in combination with a subsolar ^{16}O abundance can provide a good match to the observations. Finally, to maintain the protostellar $^{18}\text{O}/^{17}\text{O}$ in agreement with the values typically measured in nearby molecular clouds, we also infer a moderate enhancement of the initial ^{17}O abundance.

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Appendix A: Line data

Table A.1. Molecular lines of $^{12}\text{C}^{16}\text{O}$ (selection), $^{12}\text{C}^{17}\text{O}$, $^{12}\text{C}^{18}\text{O}$, $^{13}\text{C}^{16}\text{O}$, and ^{16}OH used in the analysis.

Molecule ^a	Transition	wavelength ^b [Å]	E ^c [cm ⁻¹]	gf
$^{12}\text{C}^{16}\text{O}$	2-0 R1	23432.693	3.845	1.802E-07
	4-2 R41	23540.840	7492.257	2.962E-05
	4-2 R60	23547.324	11086.589	4.871E-05
	4-2 R38	23553.885	7043.948	2.698E-05
	4-2 R24	23664.988	5390.375	1.583E-05
	3-1 R4	23667.714	2181.369	1.392E-06
	2-0 P9	23680.105	172.978	7.605E-07
$^{12}\text{C}^{17}\text{O}$	2-0 R14	23502.671	393.276	1.407E-06
	2-0 R30	23316.224	1737.760	3.223E-06
	2-0 R29	23324.897	1625.950	3.099E-06
	2-0 R28	23333.966	1517.827	2.976E-06
	2-0 R26	23353.313	1312.658	2.735E-06
$^{12}\text{C}^{18}\text{O}$	2-0 R23	23656.947	1009.011	2.298E-06
$^{13}\text{C}^{16}\text{O}$	2-0 R68	23501.045	8501.143	8.980E-06
	2-0 R69	23507.818	8747.480	9.172E-06
	2-0 R70	23515.015	8997.172	9.367E-06
	2-0 R71	23522.680	9250.210	9.565E-06
	2-0 R76	23567.025	10565.262	1.059E-05
	2-0 R19	23660.695	697.622	1.878E-06
^{16}OH	4-2 P _{1f} 6.5	16477.325	7683.8196	1.800E-05
	2-0 P _{1f} 16.5	16460.532	4915.1296	1.114E-05
	2-0 P _{2e} 15.5	16452.548	4939.7718	1.047E-05

Notes. ^(a) CO line data from Goorvitch (1994); OH lines from Rothman et al. (2009) ^(b) vacuum ^(c) lower state term energy